Guess paper Annual 2022



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صرون۔ پہندرہ دن کے اندر بورڈامتحان کی مکسل تیاری کریں

Mathematics

اب فیل ہونا بھول جائنیں۔

امتحان میں + کے گریڈی %100 گارنی

☆ بیپر Setter کے ذہن کو مد نظر رکھ کر تیار کیے گئے سوالات

یادر کھیں! اب وقت انتہائی کم رہ گیاہے۔
کے اندر بورڈ امتحان کی کمل تیاری کریں

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QUESTION NO. 2

- 1) Prove the rules of addition. $\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$
- 2) Prove the rules of addition. $\frac{a}{b} + \frac{c}{d} = \frac{ad+bc}{bd}$
- 3) Prove that $-\frac{7}{12} \frac{5}{18} = \frac{21 10}{36}$
- 4) Find the sum, difference and product of the complex numbers (8,9) and (5,-6)
- 5) Simplify: $(-1)^{\frac{-21}{2}}$
- 6) Simplify (2,6)(3,7)
- 7) Simplify (2,6) ÷ (3,7) Hint: $\frac{(2,6)}{(3,7)} = \frac{2+6i}{3+7i} \times \frac{3-7i}{3-7i}$ etc.
- 8) Simplify $(5, -4) \div (-3, -8)$
- 9) Find the multiplicative inverse of the numbers: (-4,7)
- 10) Find the multiplicative inverse of the numbers: $(\sqrt{2}, -\sqrt{5})$
- 11) Factorize: $9a^2 + 16b^2$
- 12) Factorize: $3x^2 + 3y^2$
- 13) Separate into real and imaginary parts (write as a simple complex number) $\frac{2-7i}{4+5i}$
- 14) Find the multiplicative Inverse of each of the numbers. (1,2)
- 15) Prove that $\bar{z} = z$ if z is real.
- 16) Simplify by expressing in the from a + bi $(2 + \sqrt{-3})(3 + \sqrt{-3})$
- 17) Show that $\forall z \in C$. $z^2 + \bar{z}^2$ is a real number
- 18) Show that $\forall z \in C$. $(z \bar{z})^2$ is a real number
- 19) Simplify: $\left(-\frac{1}{2} + \frac{\sqrt{3}}{2}i\right)^3$
- 20) Find moduli of the complex numbers: $1 i\sqrt{3}$
- 21) Write two proper subsets of the set: $\{a, b, c\}$
- 22) Write down the power set of the each of the sets: {+, -, ÷, ×}
- 23) Write the converse, inverse and contrapositive of the conditionals: $\sim p \rightarrow q$
- 24) Find x and y if $\begin{bmatrix} x + 3 & 1 \\ +3 & 3y 4 \end{bmatrix} = \begin{bmatrix} y & 1 \\ -3 & 2x \end{bmatrix}$
- 25) | xiv) | f A = $\begin{bmatrix} 1 & 2 \\ a & b \end{bmatrix}$ and $A^2 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$, find the values of a and b.
- 26) if A and B are square matrices of the same order, then explain why in general: $(A + B)(A B) \neq A^2$ B^2
- 27) solve the equation $\begin{bmatrix} 5 & -2 & -4 \\ 3 & -1 & -3 \\ -2 & 1 & 2 \end{bmatrix}$
- 28) without expansion show that $\begin{bmatrix} 6 & 7 & 8 \\ 3 & 4 & 5 \\ 2 & 3 & 4 \end{bmatrix} = 0$
- 29) Without expansion show that $\begin{vmatrix} 1 & 1 & 1 \\ x & y & z \\ yz & zx & xy \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ x & y & z \\ x^2 & y^2 & z^2 \end{vmatrix}$

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30) Show that
$$\begin{vmatrix} 1 & a^2 & \frac{a}{bc} \\ 1 & b^2 & \frac{b}{ca} \\ 1 & c^2 & \frac{c}{ab} \end{vmatrix} = 0$$

31) Without expansion verify that
$$\begin{vmatrix} 1 & a^2 & \frac{a}{bc} \\ 1 & b^2 & \frac{b}{ca} \end{vmatrix}$$



- 33) Salve the equation by factorization: $\frac{a}{ax-1} + \frac{b}{bx-1} = a + b; x \neq \frac{1}{a}, \frac{a}{b}$
- 34) Show that: $x^3 y^3 = (x y)(x \omega y)(x \omega^2 y)$
- 35) Evaluate: $(1 + \omega \omega^2)(1 \omega + \omega^2)$
- 36) Evaluate: $(1 + \omega \omega^2)^8$
- 37) Evaluate: $(-1 + \sqrt{-3})^5 + (-1 \sqrt{3})^5$
- 38) Solve the equations: $2x^4 32 = 0$
- 39) Salve the equations: $x^3 + x^2 + x + 1 = 0$
- 40) Use the factors theorem to determine if the first polynomial is a factor of the second polynomial. $\omega + 2.2\omega^3 + \omega^2 4\omega + 7$
- 41) Find four fourth roots of 16
- 42) If w is a cube root of unity, form an equation whose roots are 2ω and $2\omega^2$
- 43) Find roots of the equation by using quadratic formula: $15x^2 + 2ax a^2 = 0$ $\frac{1}{a^2} + \frac{1}{\beta^2}$
- 44) If α , β are the raots of $3x^2-2x+4=0$, find the values of $\frac{\alpha}{\beta}+\frac{\beta}{\alpha}$
- 45) If α , β are the raots of $3x^2 2x + 4 = 0$, find the values of $\alpha^2 \beta^2$
- 46) if a, β are the roots of $x^2 px p c = 0$, prove that $(1 + d)(1 + \beta) = 1 c$
- 47) if α, β are the roots of the equation $\alpha x^2 + bx + c = 0$, from the equation whose raots are. α^2, β^2
- 48) If α , β are the raots of the equation $ax^2 + bx + c = 0$, fram the equation whose r0ots are. $\alpha + \frac{1}{\alpha}$, $\beta + \frac{1}{\beta}$
- 49) Discuss the nature of the raots of the equation. $x^2 5x + 6 = 0$
- 50) Discuss the nature of the roots of the equation. $25x^2 30x + 9 = 0$ $x^2 2\left(m + \frac{1}{m}\right)x + 3$; $m \neq 0$
- 51) Show that the roots of the equation will be rational: $(p+q)x^2 px q = 0$
- 52) Find two consecutive numbers, whose product is 132. (Hint: Suppose the numbers are x and x + 1)
- 53) Use synthetic division to find the quotient and the remainder when the polynomial $x^4 10x^2 2x + 4$ is divided by x + 3
- 54) Discuss the nature of the raots of the equations: $2x^2 + 5x 1 = 0$
- 55) Which of the following sets have closure property w.r.t addition and multiplication ? (i) $\{0, -1\}$ (ii) $\{1, -1\}$
- 56) Theorems: $\forall z, z_1, z_2 \in Cz\bar{z} = |z|^2$
- 57) Theorems $\forall z, z_1, z_2 \in C\left(\frac{z_1}{z_2}\right) = \frac{\overline{z_1}}{\overline{z_2}}$
- 58) Find the power set $\{\{a, b\}, \{b, c\}, \{d, e\}\}$.
- 59) Reversal law of inverse if a, b are elements of group G, then show that $(ab)^{-1}b^{-1}a^{-1}$

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- 60) Find x and y if $\begin{bmatrix} x+3 & 1 \\ -3 & 3y-4 \end{bmatrix} = \begin{bmatrix} y & 1 \\ -3 & 2x \end{bmatrix}$
- 61) Solve the equation $x^{\frac{1}{2}} x^{\frac{1}{4}} 6 = 0$
- 62) Solve the equation $x^{\frac{2}{5}} + 8 = 6x^{\frac{1}{5}}$
- 63) Prove Three Cube Roots of Unity.
- 64) The Sum of all the three cube roots of unity is zero. i.e., $1 + \omega + \omega^2 = 0$

QUESTION NO. 3

- 65) Resolve the following into Partial Fraction: $\frac{6x^3 + 5x^2 7}{2x^2 x 1}$
- 66) Resolve the Partial Fraction: $\frac{9}{(x+2)^2(x-1)}$
- 67) Resolve, $\frac{7x+25}{(x+3)(x+4)}$ into Partial Fractions.
- 68) Write the first four terms of the sequences, if $a_n = (-1)^n (2n-3)$
- 69) Write the first four terms of the sequences, if $a_n = na_{n-1}$, $a_1 = 1$
- 70) Find the indicated term of the sequence: $1-3.5, -7.9, +11, \dots a_8$
- 71) Find the 13 th term of the sequence x, 1,2 -x, 3 -2x,
- 72) Which term of the A.P. -2,4,10, ... is 148?
- 73) Resolve the Partial Fraction: $\frac{x^2}{(x-2)(x-1)^2}$
- 74) Resolve, $\frac{x^2+x-1}{(x+2)^3}$ into Partial Fractions.
- 75) Write the first four terms of the sequences, if $a_n = (-1)^n n^2$
- 76) Write the first four terms of the sequences, if $a_n = \frac{n}{2n+1}$
- 77) Write the first four terms of the sequences, if $a_n a_{n-1} = n + 2$, $a_1 = 2$
- 78) If $a_{n-3} = 3n 5$, find the nth term of the sequence.
- 79) Which term of the A.P. 5,2, -1, ... is -85?
- 80) How many terms are there in the A.P. in which $a_1 = 11$, $a_n = 68$, d = 3?
- 81) If the nth term of the A.P. is 3n 1, find the A.P.
- 82) xxvii) If $\frac{1}{a}$, $\frac{1}{b}$ and $\frac{1}{c}$ are in A.P., show that $b = \frac{2ac}{a+c}$
- 83) Sum the series $\frac{3}{\sqrt{2}} + 2\sqrt{2} + \frac{5}{\sqrt{2}} + \dots + a_{13}$
- 84) Sum the series $1+4-7+10+13-16+1922-25+\cdots$ to 3 n terms
- 85) Find the 11 th term of the sequence, 1+i, 2, $\frac{4}{1+i}$
- 86) Find G.M. between -2 and 8
- 87) For what value of n, $\frac{a^n + b^n}{a^{n-1} + b^{n-1}}$ is the positive geometric mean between a and b
- 88) Find the 9th term of the harmonic sequence $\frac{-1}{5}$, $\frac{-1}{3}$, -1, ...
- 89) Iv) If 5 is the harmonic mean between 2 and b, findxxvi) Find the nth term of the sequence, $\left(\frac{4}{3}\right)^2$, $\left(\frac{7}{3}\right)^2$, $\left(\frac{10}{3}\right)^2$,
- 90) Find $A \cdot M$. between x 3 and x + 5

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- 91) Find three A. Ms between 3 and 11.
- 92) Sum the series $1.11 + 1.41 + 1.71 + \dots + a_{10}$
- 93) How many terms of the series $-7 + (-5) + (-3) + \cdots$ amount to 65?
- 94) Find the 12 th term of 1 + I, 2i, -2 + 2i, ...
- 95) Find G.M. between -2i and 8i
- 96) Insert two G.Ms. between 1 and 16
- 97) Find the 9th term of the harmonic sequence $\frac{1}{3}$, $\frac{1}{5}$, $\frac{1}{7}$, ...
- 98) The first term of an H.P. is $-\frac{1}{3}$ and the fifth term is $\frac{1}{5}$. Find its 9th term.
- 99) If A, G and h are the arithmetic, geometric and harmonic means between a and b respectively, show that $G^2 = AH$
- 100) Find A, G, H and show that $G^2 = A \cdot H$. if (i) a = -2, b = 8 (ii) a = 2i, b = 4i (iii) a = 9, b = 4
- 101) Find the sequence if $a_n a_{n-1} = n + 1$ and $a_4 = 14$
- 102) If $a_{n-2} = 3n 11$, find the nth term of the sequence.
- 103) Find the sum of the infinite G.P. 2, $\sqrt{2}$, 1, ...
- 104) Write in the factorial form: n(n-1)(n-2)...(n-r+1)
- 105) Write in the factorial form: $\frac{(n+1)(n)(n-1)}{2}$
- 106) Find the value of n when: ${}^{n}P_{2} = 30$,
- 107) Find the value of *n* when: ${}^{n}P_{4}$: $n^{-1}P_{3} = 9$: 1
- 108) How many arrangements of the letters of the words, taken all together, can be made: i) PAKPATTAN ii) PAKISTAN
- 109) In how many ways can 4 keys be arranged on a circular key ring?
- 110) Find A, G, H and verify that A > G > H (G > 0), if (i) a = 2, b = 8 (ii) $a = \frac{2}{5}, b = \frac{8}{5}$
- 111) Find the number of terms in the A.P. if: $a_1 = 3$, d = 47 and $a_n = 59$
- 112) Find three A.Ms between $\sqrt{2}$ and $3\sqrt{2}$.
- 113) Find the nth and 8 th terms of H.P; $\frac{1}{2}, \frac{1}{e^2}, \frac{1}{e}, \dots$
- 114) Evaluate: 4!2!
- 115) Write in the factorial form: (n+2)(n+1)(n)
- 116) Find the value of *n* when: ${}^{11}P_n = 11.10.9$
- 117) How many signals can be given by 5 flags of different colours, using 3 flags at a time?
- 118) How many arrangements of the letters of the words, taken all together, can be made: i) MATHEMATICS ii) ASSASSINATION
- 119) How many nacklaces can be made from 6 beads of different colours?
- 120) Evaluate: "C4
- 121) Find the value of n, when ${}^{n}C_{10} = \frac{12 \times 11}{21}$
- 122) Find the value of n and r, when ${}^nC_r=35$ and ${}^nP_r=210$
- 123) Experiment: A die is rolled. The top shows Events Happening: (i) 3 or 4 dots (ii) dots less than 5.
- 124) Two dice are thrown. What is the probability that the sum of the number of dots appearing on them is 4 or 6?
- 125) If ${}^{n}C_{8} = {}^{n}C_{12}$, find n.
- 126) A die is rolled. What is the probability that the dots on the top greater than 4?
- 127) Using the binomial theorem expand: $(a + 2 b)^5$
- 128) Find the value of n, when ${}^{n}C_{5} = {}^{n}C_{4}$

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- 129) Find the value of n, when ${}^{n}C_{12} = {}^{n}C_{6}$
- 130) What is the probability that a slip of numbers divisible by 4 is picked from the slips bearing number 1,2,3, ...,10?
- 131) Using binomial theorem, find the values to three places of decimals $\sqrt{99}$
- 132) Evaluate $\sqrt[8]{30}$ correct to three places of decimal.
- 133) If $y = 1. +2x + 4x^2 + 8x^3 + \cdots$ Show that $x = \frac{y-1}{2y}$
- 134) Expand up to four terms taking the values of x such that the expansion in each is valid. $(1 x)^{\frac{1}{2}}$
- 135) Using binomial theorem, find the values to three places of decimals $(1.03)^{\frac{1}{2}}$
- 136) If a, b, c, d are in G.P, prove that $a^2 b^2$, $b^2 c^2$, $c^2 d^2$ are in G.P.

QUESTION NO. 4

- 137) Express the sexagesimal measures of angles in redians: 75°6'30"
- 138) Convert the following radian measures of angles into the measures of sexagesimal system: $\frac{2\pi}{3}$
- 139) Find I, when: $\theta = 65^{\circ}20'$, r = 18 mm
- 140) Verify: $\sin^2 \frac{\pi}{6}$: $\sin^2 \frac{\pi}{4}$: $\sin^2 \frac{\pi}{3}$: $\sin^2 \frac{\pi}{2} = 1$: 2: 3: 4.
- 141) What is the circular measure of the angle between the hands of a watch at 4 O'clock?
- 142) Find I, when: $\theta = \pi$ radians, r = 6 cm
- 143) Find r, when: I = 5 cm, $\theta = \frac{1}{2}$ radian
- 144) Verify: $60\cos 30^{\circ} \cos 60^{\circ} \sin 30^{\circ} = \sin 30^{\circ}$
- 145) Verify: $\sin^2 \frac{\pi}{6}$: $\sin^2 \frac{\pi}{3}$: $\tan^2 \frac{\pi}{4} = 2xxiii$) Verify: $2\sin 45^\circ + \frac{1}{2}\csc 45^\circ = \frac{3}{\sqrt{2}}$
- 146) Evaluate: $\frac{1-\tan^2\frac{\pi}{4}}{1+\tan^2\frac{\pi}{3}}$
- 147) Verify the following when $\theta = 30^\circ, 45^\circ$ $\cos 2\theta = 2\cos^2 \theta 1$
- 148) Prove the following identities, state the domain of θ in each case: $\sec^2 \theta \csc^2 \theta = \tan^2 \theta \cot^2 \theta$
- 149) Prove the following identities, state the domain of θ in each case: $(\sec \theta + \tan \theta)(\sec \theta \tan \theta) = 1$
- 150) Prove the following identities, state the domain of θ in each case: $\cos^2 \theta \sin^2 \theta = \frac{1-\tan^2 \theta}{1+\tan^2 \theta}$
- 151) Prove the following identities, state the domain of θ in each case: $\frac{\sin \theta}{1+\cos \theta} + \cot \theta = \csc \theta$
- 152) Prove the following identities, state the domain of θ in each case: $\frac{\cot^2 \theta 1}{1 + \cot^2 \theta} = 2\cos^2 \theta 1$
- 153) xivii) Prove that $\cos^2 \theta \sin^4 \theta = \cos^2 \theta \sin^2 \theta$,
- 154) Verify the following when $\theta=30^\circ, 45^\circ \sin 2\theta=2\sin \theta \cos \theta$
- 155) Find x, if $\tan^2 45^\circ \cos^2 60^\circ = x \sin 45^\circ \cos 45_0 \tan 60^\circ$
- 156) Prove the following identities, state the domain of θ in each case: $\frac{\cos \theta \sin \theta}{\cos \theta + \sin \theta} = \frac{\cot \theta 1}{\cot \theta + 1}$
- 157) Prove the following identities, state the domain of θ in each case: $\frac{1+\cos\theta}{1+\cos\theta} = (\csc\theta + \cot\theta)^2$
- 158) Prove that: $\sqrt{\frac{1-\sin\theta}{1+\sin\theta}} = \sec\theta \tan\theta$, where
- 159) Show that: $\cot^4 \theta + \cot^2 \theta = \csc^4 \theta \csc^2 \theta$ where θ is not an integral multiple of $\frac{\pi}{2}$

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- 160) Prove: $\sin 780^{\circ} \sin 480^{\circ} + \cos 120^{\circ} \sin 30^{\circ} = \frac{1}{2}$
- 161) Prove that: $tan(45^{\circ} + A)tan(45^{\circ} + A) = 1$
- 162) Prove that: $\frac{1-\tan\theta\tan\theta}{1+\tan\theta\tan\theta} = \frac{\cos(\theta+\theta)}{\cos(\theta-\theta)}$
- 163) Prove that: $\frac{\cos 8^{\circ} \sin 8^{\circ}}{\cos 8^{\circ} + \sin 8^{\circ}} = \tan 37^{\circ}$
- 164) Prove the identities: $\cot \alpha \tan \alpha = 2 \cot 2\alpha$
- 165) Prove the identities: $1 + \tan \alpha \tan 2\alpha = \sec 2\alpha$
- 166) Express the products as sums or differences: $2\sin 3\theta\cos\theta$
- 167) Prove: $\sin(180^{\circ} + \alpha)\sin(90 \alpha) = -\sin\alpha\cos\alpha$
- 168) If α , β , γ are the angles of a triangle ABC, then prove that: $\cos(\alpha + \beta) = \cos \gamma$
- 169) Find the values: $\sin 105^\circ$ lxviii) Prove that: $\cos(\alpha + 45^\circ) = \frac{1}{\sqrt{3}}(\cos \alpha \sin \alpha)$
- 170) Prove that: $\sin\left(\theta + \frac{\pi}{6}\right) + \cos\left(\theta + \frac{\pi}{3}\right) = \cos \theta$
- 171) Show that: $\cot(\alpha + \beta) = \frac{\cot \alpha \cot \beta 1}{\cot \alpha + \cot \beta}$
- 172) Find the values of $\sin 2\alpha$, $\cos 2\alpha$ and $\tan 2\alpha$, when: $\cos \alpha = \frac{3}{2}$, where $0 < \alpha < \frac{\pi}{2}$
- 173) Prove the identities: $\frac{\sin 2\alpha}{1 + \cos 2\alpha} = \tan \alpha$ 174) Prove the identities: $\frac{2\sin \theta \sin 2\theta}{\cos \theta + \cos 3\theta} = \tan 2\theta \tan \theta$
- 175) Express the sums or differences as products: $\sin(x + 30^\circ) + \sin(x 30^\circ)$
- 176) Express $\sin 5x + \sin 7x$ as a product.
- 177) Find the periods of the functions: tan 4x
- 178) Find the periods of the functions: sin =
- 179) Solve the right triangle ABC, in which $\gamma = 90^{\circ}$ a = 3.28, b = 5.74
- 180) At the top of a cliff 80 m high, the angle of depression of a boat is 12°. How far is the boat from
- 181) the cliff?
- 182) When the angle between the ground and the sun is 30° , flag pole casts a shadow of 40 m long. Find the height of the flag.
- 183) Solve the triangle ABC in which: $a = \sqrt{3} 1$, $b = \sqrt{3} + 1$ and $\gamma = 60^{\circ}$
- 184) Solve the triangle ABC in which: a = 7, b = 3 and $\gamma = 38^{\circ}13'$
- 185) Prove that: $\frac{\sin A + \sin 2A}{1 + \cos A + \cos 2A} = \tan A$
- 186) Find the periods of the functions: $\cos 2x$
- 187) Solve the triangles, in which: a = 32, b = 40, c = 66
- 188) Find the smallest angle of the triangle ABC, When a = 37.34, b = 3.24, c = 35.06
- 189) Find the area of the triangle ABC, given two sides and their included angle: $b=37, c=45, \alpha=$ 30°50'
- 190) Show that: $r_2 = 4R\cos\frac{\alpha}{2}\sin\frac{\beta}{2}\cos\frac{\gamma}{2}$
- 191) Prove that: $rr_1r_2r_3 = \Delta^2$
- 192) Find R, r, r1, r2 and r3, if measures of the
- 193) sides of triangle ABC are a = 34, b = 20, c = 42
- 194) Prove that in an equilateral triangle. r: R: r_1 : r_2 : r_3 = 1: 2: 3: 3: 3
- 195) Prove that: $(r_1 + r_2) \tan \frac{\gamma}{2} = c$.
- 196) Evaluate without using tables / calculator: $\cos^{-1}\left(\frac{\sqrt{3}}{2}\right)$

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- 197) Without using table / Calculator show that: $2\cos^{-1}\frac{4}{5} = \sin^{-1}\frac{24}{25}$
- 198) Find the area of the triangle ABC, given one side and two angles: b=25.4, $\gamma=36^{\circ}41'$, $\alpha=45^{\circ}17'$
- 199) Find the area of the triangle ABC, given three sides: $a=18,\ b=24$, c=30
- 200) Show that: $r_3 = 4R\cos\frac{\alpha}{2}\cos\frac{\beta}{2}\sin\frac{\gamma}{2}$
- 201) Prove that: $r_1 r_2 r_3 = r s^2$
- 202) Prove that in an equilateral triangle. r: R: $r_1 = 1:2:3$
- 203) Prove that: $abc(\sin \alpha + \sin \beta + \sin \gamma) = 4\Delta s$
- 204) Prove that: $(r_3 r)\cot \frac{\gamma}{2} = c$.
- 205) Without using table / Calculator show that: $\tan^{-1} \frac{5}{12} = \sin^{-1} \frac{5}{13}$
- 206) Find the value of each expression: $\sin\left(\sin^{-1}\left(\frac{1}{2}\right)\right)$
- 207) Show that: $\sin(2\cos^{-1}x) = 2x\sqrt{1-x^2}$
- 208) Show that: $\cos^{-1}(-x) = \pi \cos^{-1} x$
- 209) Solve the trigonometric equations: $\sec^2 \theta = \frac{4}{3}$
- 210) Find the values of θ satisfying the equations: $3\tan^2\theta + 2\sqrt{3}\tan\theta + 1 = 0$
- 211) Solve: $\sin x + \cos x = 0$
- 212) Prove that $\sec^2 A + \csc^2 A = \sec^2 A \csc^2 A$
- 213) Show that: $\sin^{-1}(-x) = -\sin^{-1}x$
- 214) Show that: $tan(sin^{-1}x) = \frac{x}{\sqrt{1-x^2}}$
- 215) Show that $\cos^{-1}\frac{12}{13} = \sin^{-1}\frac{5}{13}$
- 216) Prove that $(\sec \theta \tan \theta)^2 = \frac{1-\sin \theta}{1+\sin \theta}$
- 217) Prove that : $R = \frac{abc}{4\Delta}$

LONG Q.NO. 5

- 1) Reversal law of inverse if a ,b are elements of group G , then show that $(ab)^{-1} = b^{-1}a^{-1}$
- 2) If G is a group under the operation x and $a,b \in G$, find the solutions of the equation. a * x = b, x * a = b
- 3) Show that the set $\{1, \omega, \omega^2\}$, when $\omega^3 = 1$, is an Abelian group w.r.t. ordinary multiplication.
- 4) Show that $\begin{vmatrix} a+l & a & a \\ a & a+l & a \\ a & a+l \end{vmatrix} = l^2(3a+l)$
- $3x_1 + x_2 x_3 = -4$ 5) Use Crammer's rule to solve the system. $x_1 + x_2 2x_3 = -4$ $-x_1 + 2x_2 x_3 = 1$
- 6) Show that $\begin{vmatrix} a+\lambda & b & c \\ a & b+\lambda & c \\ c & c+\lambda \end{vmatrix} = \lambda^2 (\mathbf{a} + \mathbf{b} + \mathbf{c})$
- 7) Solve the equation by Cramer's rule. $\begin{cases} 2x_1 + 2x_2 + x_3 = 8 \\ x_1 + 2x_2 + 2x_3 = 6 \\ x_1 2x_2 x_3 = 1 \end{cases}$
- 8) Find the value of λ for the system of non-trivial solution . Also solve the system for the value of λ

$$\begin{cases} x_1 + 4x_2 + \lambda x_3 = 0 \\ 2x_1 + x_2 - 3x_3 = 0 \\ 3x_1 + \lambda x_2 - 4x_3 = 0 \end{cases}$$

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- $(2x_1 + 2x_2 + x_3 = 8)$ 9) Solve the system of linear equation by Cramer's rule $\{x_1 + 2x_2 + 2x_3 = 6\}$ $(x_1 - 2x_2 - x_3 = 1)$ $2x_1 + x_2 + 3x_3 = 3$
- 10) Use matrices to solve the system $\begin{cases} x_1 + x_2 2x_3 = 0 \end{cases}$

LONG O.NO. 6

- 11) Solve the equation (x+1)(2x+3)(2x+5)(x+3) = 945
- 12) Solve the equation $4.2^{2\alpha+1} 9.2^x + 1 = 0$
- 13) Solve the equation $3^{2x-1} 12.3^x + 81 = 0$
- 14) Solve the equation $\left(x + \frac{1}{x}\right)^2 3\left(x + \frac{1}{x}\right) 4 = 0$
- 15) Solve the equation: $(x+4)(x+1) = \sqrt{x^2 + 2x 15} + 3x + 31$
- 16) Prove that complex cube roots of -1 are $\frac{1+\sqrt{3}i}{2}$ and $\frac{1-\sqrt{3}i}{2}$; and hence prove that $\left(\frac{1+\sqrt{-3}i}{2}\right)^9+\left(\frac{1-\sqrt{-3}}{2}\right)^9=$
- 17) If the roots of $px^2 + qx + q = 0$ are α and \betathen prove that $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} + \sqrt{\frac{q}{p}} = 0$ Show that the roots of $x^2 + (mx + c)^2 = a^2$ will be equal, if $c^2 = a^c(1 + m^2)$ xoix) Prove that $\frac{x^2}{a^2} + \frac{(mx + c)^2}{b^2} = 1$ will have equal roots, if $c^2 = a^2m^2 + b^2$; $a \neq 0, b \neq 0$
- 18) Resolve the Partial Fraction: $\frac{x-1}{(x-2)(x+1)^9}$ 19) Resolve the Partial Fraction: $\frac{2x+1}{(x+3)(x-1)(x+2)^2}$ 20) Resolve the Partial Fraction: $\frac{9x-7}{(x^2+1)(x+3)}$

- 21) xlv) Resolve the Partial Fraction: $\frac{x^2+1}{x^3+1}$
- 22) xlvi) Resolve the Partial Fraction: $\frac{1}{(x-1)^2(x^2+2)}$
- 23) Resolve, $\frac{1}{(x+1)^2(x^2-1)}$ into Partial Fractions.
- 24) Resolve, $\frac{4x^2}{(x^2+1)^2(x-1)}$ into Partial Fractions.

LONG Q.NO. 7

- 25) Find n so that $a^{n+b^{n}}$ may be the A.M. between a and b.
- The sum of three numbers in an A.P. is 24 and their product is 440. Find the numbers.
- Find four numbers in A.P. whose sum is 32 and the sum of whose squares is 276.
- 28) Find the five numbers in A.P. whose sum is 25 and the sum of whose squares is 135.
- 29) If $\frac{1}{a}$, $\frac{1}{b}$ and $\frac{1}{c}$ are in G.P. show that the common ratio is $\pm \sqrt{\frac{a}{c}}$
- 30) If there consecutive numbers in A.P. are increased by 1,4,15 respectively, the resulting numbers are in G.P.
- 31) Find the original numbers if their sum is 6.
- 32) Sum the series $2 + (1-i) + \left(\frac{1}{i}\right) + \cdots$ to 8 terms.

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 33) If $y = \frac{x}{2} + \frac{1}{4}x^2 + \frac{1}{8}x^3 + \cdots$ and if 0 < x < 2, then prove that $x = \frac{2y}{1+y}$
- 34) If $y = \frac{2}{3}x + \frac{4}{9}x^2 + \frac{8}{27}x^3 + \cdots$ and if $0 < x < -\frac{3}{2}$ then show that $x = \frac{3y}{2(1+y)}$
- 35) If the numbers $\frac{1}{k}$, $\frac{1}{2k+1}$ and $\frac{1}{4k-1}$ are in harmonic sequence, find k.
- 36) Find n so that $\frac{a^{n+1}+b^{n+1}}{a^n+b^n}$ may be H.M. between a and b
- 37) If the H.M and A.M between two numbers are 4 and $\frac{9}{4}$ respectively, find the numbers.
- 38) If the positive G.M. and H.M. between two numbers are 4 and $\frac{16}{5}$
- 39) Use mathematical induction to prove the formula for every positive integer n. $1+4+7+\cdots+(3n-1)$ $2) = \frac{n(3n-1)}{3}$
- 40) Find the term involving x^4 in the expansion of $(3-2x)^7$
- 41) Find the coefficient of x^5 in the expansion of $\left(x^2 \frac{3}{2x}\right)^{10}$
- 42) Find the term independent of x in the expansion: $\left(x-\frac{2}{x}\right)^{10}$ xaxiv) Determine the middle term or terms in the expansions: $\left(\frac{1}{x} - \frac{x^2}{2}\right)^{12}$ xoxy) Determine the middle term or terms in the expansions: $\left(\frac{3}{2}x - \frac{1}{3x}\right)^{11}$
- 43) Find the coefficient of x^n in the expansion. $\frac{(1+x)^2}{(1-x)^2}$
- 44) Identify the series $1 \frac{1}{2} \left(\frac{1}{4} \right) + \frac{1.3}{2!4} \left(\frac{1}{4} \right)^2 \frac{1.3.5}{3!8} \left(\frac{1}{4} \right)^3 + \cdots$ as binomial expansion and find its sum.
- 45) Identify the series $1 \frac{1}{2} \left(\frac{1}{2}\right) + \frac{1.3}{2.4} \left(\frac{1}{2}\right)^2 \frac{1.3.5}{2.4.6} \left(\frac{1}{2}\right)^3 + \cdots$ as binomial expansion and find its sum.
- 46) If $y = \frac{1}{3} + \frac{1.3}{2!} \left(\frac{1}{3}\right)^2 + \frac{1.3.5}{3!} \left(\frac{1}{3}\right)^3 + \cdots$. Prove that $y^2 + 2y 2 = 0$ 47) If $2y = \frac{1}{2^2} + \frac{1.3}{2!} \cdot \frac{1}{2^4} + \frac{1.3.5}{3!} \cdot \frac{1}{2^6} + \cdots$ prove that $4y^2 + 4y 1 = 0$

LONG O.NO. 8

- 48) Find the values of the remaining trigonometric functions: $\cos \theta = \frac{9}{44}$ and the terminal arm of the angle is in quad. IV.
- 49) If $\csc\theta = \frac{m^2+1}{2m}$ and m>0 $\left(0<\theta<\frac{\pi}{2}\right)$, find the value of the remaining trigonometric ratios.
- 50) If $\cot \theta = \frac{5}{2}$ and the terminal arm of the angle is in the I quad., find the value of $\frac{3\sin \theta + 4\cos \theta}{\cos \theta \sin \theta}$.
- 51) Prove the following identities, state the domain of θ in each case:
- 52) $\sin^3 \theta \cos^3 \theta = (\sin \theta \cos \theta)(1 + \sin \theta \cos \theta)$
- 53) Prove the following identities, state the domain of θ in each case:
- 54) $\sin^6 \theta \cos^6 \theta = (\sin^2 \theta \cos^2 \theta)(1 + \sin^2 \theta \cos^2 \theta)$
- 56) Show that $\cos(\alpha + \beta) + \sin(\alpha \beta) = \cos^2 \alpha \sin^2 \beta = \cos^2 \beta \sin^2 \alpha$
- 57) Find $\sin(\alpha + \beta)$ and $\cos(\alpha + \beta)$, given that: $\tan \alpha = \frac{3}{4}$, $\cos \beta = \frac{5}{13}$ and neither the terminal side of the angle of measure α nor that of β is in the I quadrant.
- 58) Prove the identities: $\sqrt{\frac{1+\sin\alpha}{1-\sin\alpha}} = \frac{\sin\frac{\alpha}{2}+\cos\frac{\alpha}{2}}{\sin\frac{\alpha}{2}-\cos\frac{\alpha}{2}}$

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- 59) Prove the identities: $\frac{\cos 3\theta}{\cos \theta} + \frac{\sin 3\theta}{\sin \theta} = 4\cos 2\theta$
- 60) Prove the identities: $\frac{\sin 8x + \sin 2x}{\cos 8x + \cos 2x} = \tan 5x$
- 61) Prove the identities: $\frac{\sin \alpha \sin \beta}{\sin \alpha + \sin \beta} = \tan \frac{\alpha \beta}{2} \cot \frac{\alpha + \beta}{2}$

LONG Q.NO. 9

- 62) Solve the right triangle ABC, in which $\gamma = 90^{\circ} b = 68.4$, c = 96.2
- 63) Solve the triangle ABC, if $\beta = 60^{\circ}$, $\gamma = 15^{\circ}$, $b = \sqrt{6}$
- 64) Solve the triangle ABC in which: b = 95, c = 34 and $\alpha = 52^{\circ}$
- 65) Solve the triangles, using first Law of tangents and then Law of sines: b=14.8, c=16.1 and $\alpha=42^{\circ}45'$
- 66) Solve the triangles, using first Law of tangents and then Law of sines: b = 61, a = 32 and $\alpha = 59^{\circ}30$
- 67) The sides of a triangle are $x^2 + x + 1,2x + 1$ and $x^2 1$. Prove that the greatest angle of the triangle is 120° x) Show that: i) $r = 4R\sin\frac{\alpha}{2}\sin\frac{\beta}{2}\sin\frac{\gamma}{2}$ ii) $s = 4R\cos\frac{\alpha}{2}\cos\frac{\beta}{2}\cos\frac{\gamma}{2}$
- 68) Find R, r, r_1, r_2 and r_3 , if measures of the sides of triangle ABC are $\alpha = 13$, b = 14, c = 15
- 69) Prove that: $\tan^{-1}\frac{1}{4} + \tan^{-1}\frac{1}{5} = \tan^{-1}\frac{9}{19}$
- 70) Prove that: $3\tan^{-1}\frac{2}{3} = \sin^{-1}\frac{12}{13}$
- 71) Prove that: $\sin^{-1}\frac{3}{5} + \sin^{-1}\frac{8}{17} = \sin^{-1}\frac{77}{85}$
- 72) Prove that: $\tan^{-1}\frac{1}{11} + \tan^{-1}\frac{5}{6} = \tan^{-1}\frac{1}{3} + \tan^{-1}\frac{1}{2}$
- 73) Prove that: $2\tan^{-1}\frac{1}{3} + \tan^{-1}\frac{1}{7} = \frac{\pi}{4}$
- 74) Prove that : $\frac{1}{r^2} + \frac{1}{r_1^2} + \frac{1}{r_2^2} + \frac{1}{r_3^2} = \frac{a^2 + b^2 + c^2}{\Delta^2}$